

BLDE ASSOCIATION'S
S.B.ARTS AND K.C.P SCIENCE COLLEGE, VIJAYAPUR



DEPARTMENT OF MATHEMATICS

ADVANCE LEARNERS

For the Academic Year : 2015-16

BLDE ASSOCIATION'S
S.B.ARTS AND K.C.P SCIENCE COLLEGE, VIJAYAPUR



DEPARTMENT OF MATHEMATICS

Ren cla

SEMINAR REPORT


2015-16 (Even Semester)

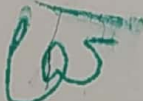
**BLDE ASSOCIATION'S
S.B.ARTS AND K.C.P SCIENCE COLLEGE, VIJAYAPUR**

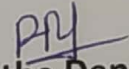
DEPARTMENT OF MATHEMATICS

NOTICE

The UG Department of Mathematics is conducting Seminar for the B.Sc students for the Academic Year 2015-16 (Even Semester).


Co-ordinator
S.B.Arts & K.C.P.Science College,
Vijayapur.


Principal,
S.B. Arts and KCP Science College,
VIJAYAPUR


Head of the Department
H. O. D.
Department of Mathematics,
S. B. Arts & K. C. P. Science
College, Vijayapur.

B.L.D.E.A's S.B.Arts & K.C.P Science College, Vijayapura

Department of Mathematics

SEMINAR – 2016 (EVEN SEMESTER)

Sl.No	Semester	Name of the students	Topics	Date
1.	II	Suvarna Gidaganti	The Sphere	07/03/2016
2.	IV	Roopanjali Bondarde	Differential equations of nth order	16/03/2016
3.	VI	Shweta Shapeti	Laplace Transformation	23/03/2016



Name : Suvarna Gidaganti

Semester : II

Topic : The sphere

B. L. D. E Association's .

S. B ARTS AND KCP SCIENCE COLLEGE

VIJAYAPURE.

DEPARTMENT OF MATHEMATICS.

Seminar on : SPHERE .

Name :- Suvarna. Gidaganti.

Class :- B.sc II Sem.

Date :- 07/03/2016

Subject :- Mathematics .

SPHERE :-

Defⁿ :- A sphere is a perfectly round geometrical object in three dimensional space that is a surface of completely round ball.

Equation of sphere :-

Let $A(a, b, c)$ be a fixed pt in space and let r be any +ve real number and let $P(x, y, z)$ be moving pt such that $AP = r$, a constant.

Squaring on both sides, we get

$$(AP)^2 = r^2$$

$$(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2$$

which is required eqⁿ of sphere with centre $A(a, b, c)$ and radius r .

Equation of sphere in standard form.

i.e eqⁿ of a sphere whose centre is the origin and radius r .

Let $O = (0, 0, 0)$ be centre of the sphere.

Let $P(x, y, z)$ be any pt on the sphere. Join OP .

Since OP is r radius of a sphere

$$OP = r$$

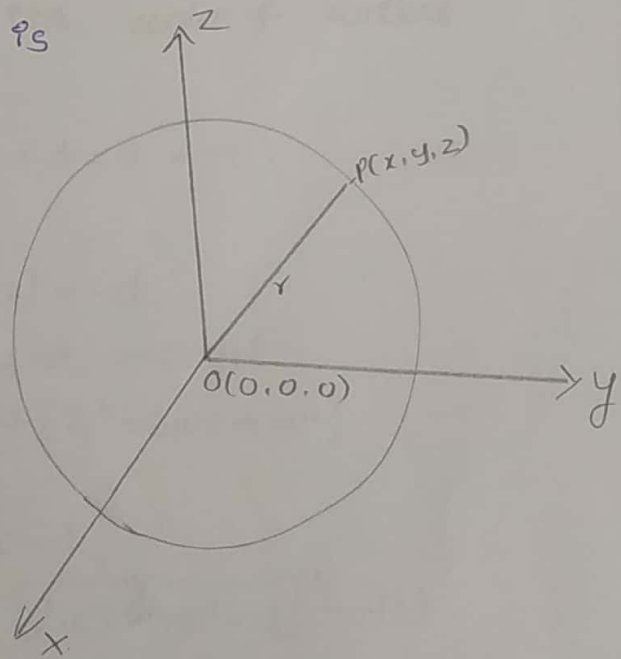
By using distance formula

$$\sqrt{(x-0)^2 + (y-0)^2 + (z-0)^2} = r$$

$$\sqrt{x^2 + y^2 + z^2} = r$$

$$\text{or } x^2 + y^2 + z^2 = r^2$$

which is required equation.



Equation of sphere in central form.

i.e eqⁿ of a sphere whose centre is (a, b, c) and the radius a .

Let $c = (a, b, c)$ be the centre of the sphere

Let $P(x, y, z)$ be any point on the sphere. Join CP .

Since $CP = r$ (given)
 $CP^2 = a^2$

by distance formula \swarrow
 x

$$(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2.$$

which is required eqⁿ.

Equation of sphere in General form.

To prove that the eqⁿ $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$ represents a sphere and find its centre & radius.

Proof: - Given eqⁿ is

$$x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0 \quad \text{--- (1)}$$

which can be rearranged as

$$(x^2 + 2ux) + (y^2 + 2vy) + (z^2 + 2wz) = -d.$$

adding both side by $u^2 + v^2 + w^2$, we get.

$$(x^2 + 2ux + u^2) + (y^2 + 2vy + v^2) + (z^2 + 2wz + w^2) = u^2 + v^2 + w^2 - d$$

$$(x+u)^2 + (y+v)^2 + (z+w)^2 = u^2 + v^2 + w^2 - d.$$

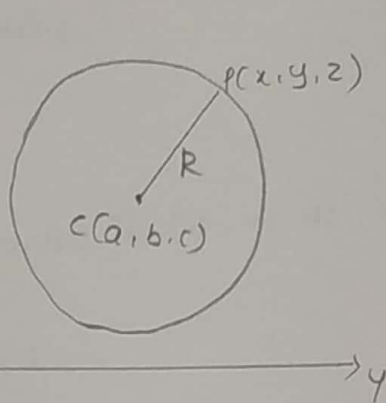
$$[x - (-u)]^2 + [y - (-v)]^2 + [z - (-w)]^2 = [\sqrt{u^2 + v^2 + w^2 - d}]^2 \quad \text{--- (2)}$$

which is of the form.

$$(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2 \quad \text{--- (3)}$$

\therefore Equation (1) represents a sphere.

Now to find centre and radius of sphere.



For that comparing eqn (2) & (3) we have

$$a = -u, b = -v, c = -w.$$

$\therefore r = \sqrt{u^2 + v^2 + w^2} - d$ is a radius.

$\therefore c = (-u, -v, -w)$ is a centre.

Examples: -

1) Find the eqn of sphere whose centre is $(2, -1, 4)$ and radius is 3 units.

Solⁿ: - $C = (2, -1, 4) = (a, b, c)$ & $r = 3$.

eqn of sphere is

$$(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2$$

put above values

$$(x-2)^2 + (y+1)^2 + (z-4)^2 = 3^2$$

$$x^2 + 4 - 4x + y^2 + 1 + 2y + z^2 + 16 - 8z = 9$$

$$x^2 + y^2 + z^2 - 4x + 2y - 8z + 21 = 9$$

$$x^2 + y^2 + z^2 - 4x + 2y - 8z + 12 = 0 //$$

2) Find the eqn of a sphere whose centre is $(0, -2, 3)$ & $(2, 6, -1)$ be a pt on the sphere.

Solⁿ: let $C(0, -2, 3)$ & $P(2, 6, -1)$

$$CP = r = \sqrt{(2-0)^2 + (6+2)^2 + (-1-3)^2}$$

$$= \sqrt{4 + 64 + 16}$$

$$r = \sqrt{84}$$

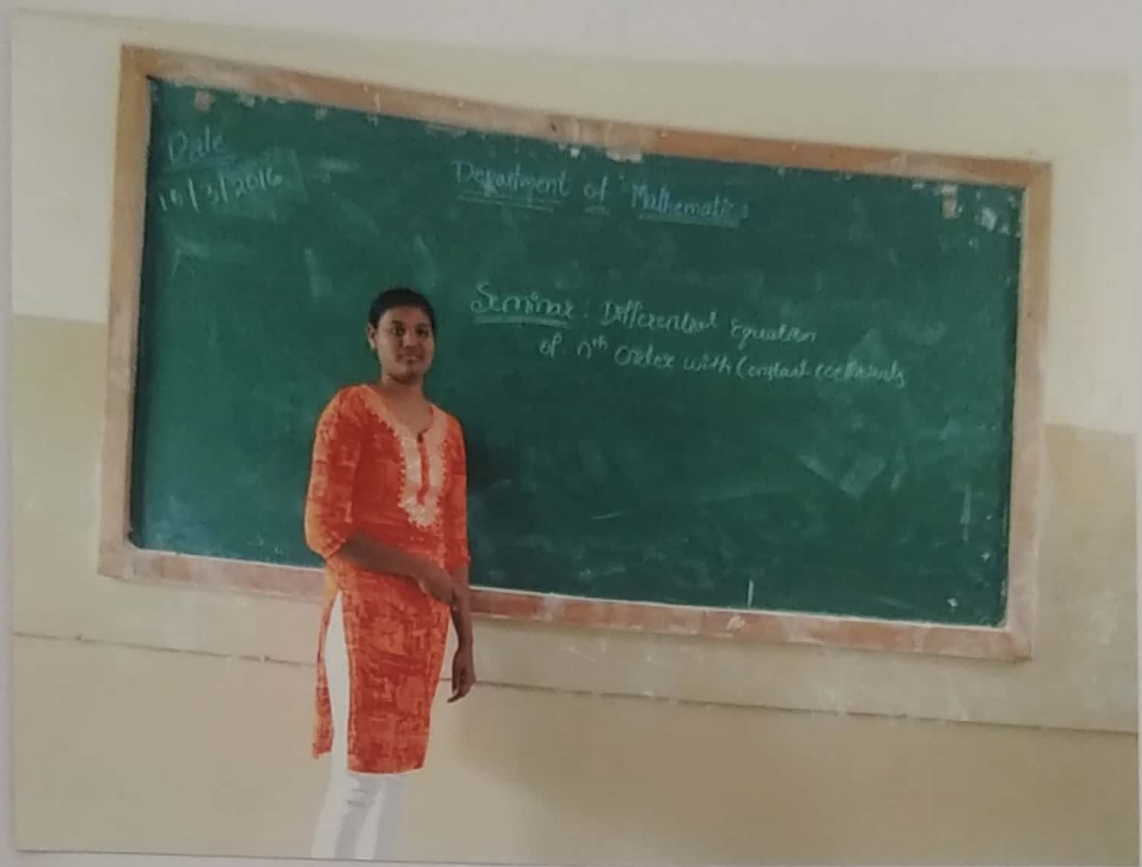
required eqn of sphere is

$$(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2$$

$$(x-0)^2 + (y+2)^2 + (z-3)^2 = (\sqrt{84})^2$$

$$x^2 + y^2 + 4 + 4y + z^2 + 9 - 6z = 84$$

$$x^2 + y^2 + z^2 + 4y - 6z - 71 = 0 //$$



Name : Roopanjali Bondarde
Semester : IV
Topic : Differential equation of
nth order

S.B. Arts & K.C.P
Science College Bijapur

Department of Mathematics

Seminar on: - Differential equations
of n^{th} order.

Name -> Reepanjali . Bondarde
Sem -> BSc IVth sem

Date -> 16-03-2016

Reg. No -> 81420642

Linear Differential Equations of order n
with constant coefficients \rightarrow

Linear differential equations constitute a highly important class of differential equations in physics & engineering & are used as idealized mathematical models of such phenomena as mathematical vibrations, electrical circuits, planetary motion etc.

Differential equations of 1st order & 1st degree & first order & higher degree have so far been discussed.

Since the general theory of L. D. E's can be dealt with differential & integral equations, a brief review of their properties is in order. The operators discussed below further properly.

* The Algebra of constant coefficient

We define operators D by

$$Dy = \frac{dy}{dx}, \quad D^2y = \frac{d^2y}{dx^2}, \quad \dots, \quad D^n y = \frac{d^n y}{dx^n}$$

Let us now verify that D is linear. If f_1 & f_2 are differentiable functions the $C_1 f_1 + C_2 f_2$ is differentiable &

$$\frac{d}{dx} (C_1 f_1 + C_2 f_2) = C_1 \frac{df_1}{dx} + C_2 \frac{df_2}{dx}$$

Where C_1 & C_2 are constant.

$$\text{But this means that } D(C_1 f_1 + C_2 f_2) = C_1 Df_1 + C_2 Df_2.$$

& D satisfies the ~~equo~~ requirement of linearity. In general, all integral powers of D are linear

$$f(D)(C_1 f_1 + C_2 f_2) = C_1 Df_1 + C_2 Df_2$$

In general, we shall be interested in $f(D)$, $\phi(D)$ being the rational functions of D . Define their sum & product by

$$[f(D) + \phi(D)]y = f(D)y + \phi(D)y$$

$$f(D)\phi(D)y = f(D)\phi[Dy]$$

We can therefore treat D , as though it is an algebraic symbol. It follows the expressions with constant coefficients can be multiplied & factored like algebraic equations.

We next define $D^{-1}y = \left(\frac{1}{D}\right)y = x$

if $Dx = y$.

The operator $\frac{1}{D}$ according to this relation is the inverse of the operator D (equivalent to 'integration') in general

$f(D)$ or $\frac{1}{f(D)}$ will represent another

operator such that $f(D)f^{-1}(D)y = y$.

~~Ex 4~~ General linear differential equations \rightarrow

The complementary function (C.F), the particular integral (P.I), the complete integral (C.I).

The general form of the linear differential equation of order n is

$$P_0 \frac{d^n y}{dx^n} + P_1 \frac{d^{n-1} y}{dx^{n-1}} + \dots + P_{n-1} \frac{dy}{dx} = P_n y + Q$$

Where P_0, P_1, \dots, P_n are constants or functions of x . By using the symbol

D , eqn (1) can be written as

$$(P_0 D^n + P_1 D^{n-1} + \dots + P_n) y = X \quad (2)$$

or $f(D)y = X$.

Equation (1) has been solved completely for $n=1$.

As there is no loss of generality from taking the leading coefficient to be unity, eqn (2) may be written as

$$(D^n + P_1 D^{n-1} + \dots + P_n) y = X \quad (3)$$

If $X=0$, the eqn is said to be homogeneous. It is important to note that

* Solve $(D^4 + 6D^3 + 5D^2 - 24D - 36)y = 0$

∴ The A.E is $m^4 + 6m^3 + 5m^2 - 24m - 36 = 0$

∴ roots of A.E are $2, -2, -3, -3$.

Hence the G.S is

$$y = C_1 e^{2x} + C_2 e^{-2x} + C_3 e^{-3x} + C_4 x e^{-3x}$$

* Solve $(D^4 - 2D^3 - 3D^2 + 4D + 4)y = 0$

\Rightarrow The A.E is $m^4 - 2m^3 - 3m^2 + 4m + 4 = 0$

$\Rightarrow m^4 - 2m^3 - 3m^2 + 6m - 2m + 4 = 0$

$\Rightarrow m^3(m-2) - 3m(m-2) - 2(m-2) = 0$

$\Rightarrow (m-2)(m^3 - 3m - 2) = 0$

$\Rightarrow (m-2)^2(m+1)^2 = 0$

The roots of A.E are 2, 2, -1, -1

The e.s is $y = e^{2x}(c_1 + c_2x) + e^{-x}(c_3 + c_4x)$

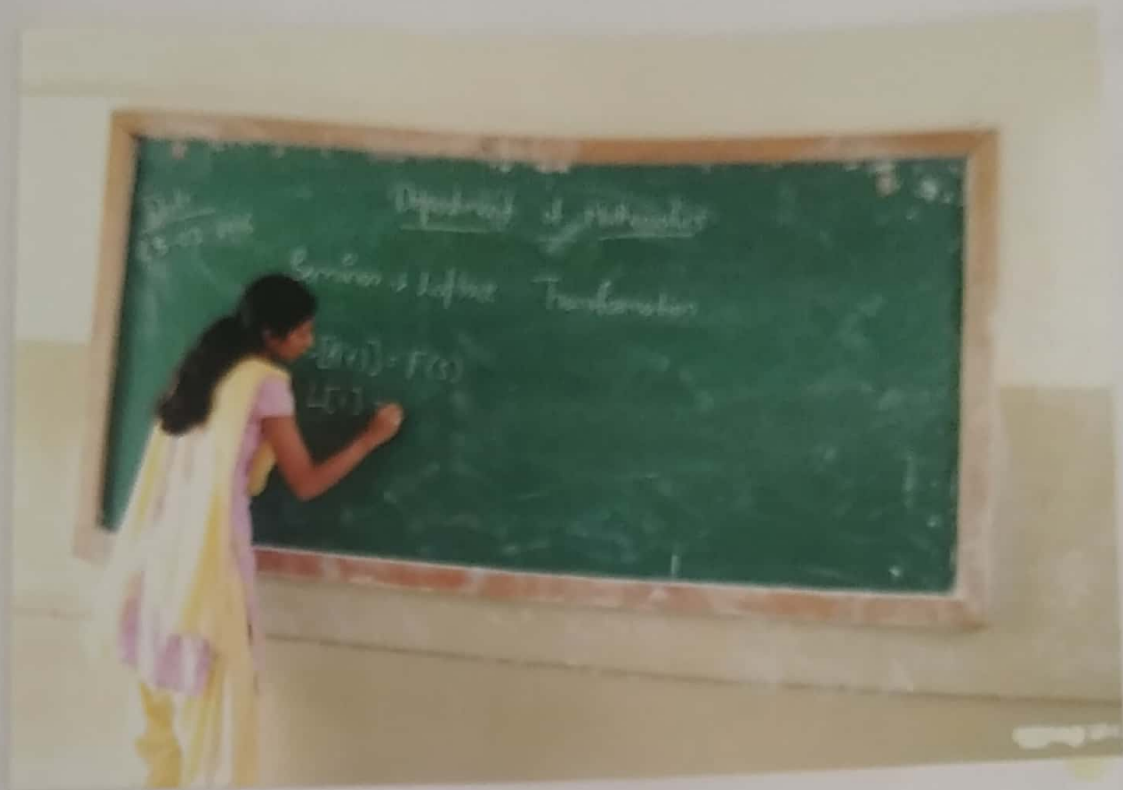
* Solve $(D^4 + 5D^2 - 36)y = 0$

\Rightarrow The A.E is $m^4 + 5m^2 - 36 = 0$

or $(m^2 - 4)(m^2 + 9) = 0$

The roots of A.E are $\pm 2, \pm 3i$ &

The e.s is $y = c_1 e^{2x} + c_2 e^{-2x} + c_3 \cos 3x + c_4 \sin 3x$



Name : Shweta Shapeti

Semester : VI

Topic : Laplace Transformation

S. B. Arts & K. C. P Science

College, Bijapur.

Seminar

Name -> Shweta. C. Shapeti

Reg. No -> 81319909

Dept. -> Mathematics

Sem -> Bsc. VIth sem.

Topic -> Laplace Transformation.

Date -> 23-03-2016.

Laplace Transform

Let $f(t)$ be a function of a real variable 't' defined for $t \geq 0$.

Laplace transform of $f(t)$ is denoted by $L[f(t)]$ and is defined by.

$$L[f(t)] = \int_0^{\infty} e^{-st} f(t) dt$$

Provided the integral on the right hand exist, where 's' is a parameter, a real or a complex number. The operator L is called Laplace transform operator.

Clearly, the $L[f(t)]$ is a function of the parameter s . we denote this function by $F(s)$

$$\text{Thus, } L[f(t)] = \int_0^{\infty} e^{-st} f(t) dt = F(s)$$

Linearity property \rightarrow

If $f(t)$ and $g(t)$ are two functions whose Laplace transforms exist and if a and b are any constants, then

Proof:- By definition of Laplace transforms
[L.T.]

$$\begin{aligned}
 L[af(t) + bg(t)] &= \int_0^{\infty} e^{-st} [af(t) + bg(t)] dt \\
 &= \int_0^{\infty} [ae^{-st} f(t) + be^{-st} g(t)] dt \\
 &= a \int_0^{\infty} e^{-st} f(t) dt + b \int_0^{\infty} e^{-st} g(t) dt \\
 &= aL[f(t)] + bL[g(t)]
 \end{aligned}$$

$$\therefore L[af(t) + bg(t)] = aL[f(t)] + bL[g(t)]$$

Transform of Elementary Functions \Rightarrow

1. $L[e^{at}]$

Soln \rightarrow By definition of L.T.

$$\begin{aligned}
 L[e^{at}] &= \int_0^{\infty} e^{-st} e^{at} dt = \int_0^{\infty} e^{-(s-a)t} dt \\
 &= \left[\frac{e^{-(s-a)t}}{-(s-a)} \right]_0^{\infty} = \frac{e^{-\infty}}{-(s-a)} - \frac{e^0}{-(s-a)}
 \end{aligned}$$

$$= 0 + \frac{1}{s-a} \quad (\because e^{-\infty} = 0 \text{ \& } e^0 = 1)$$

$$= \frac{1}{s-a}$$

$\therefore L[e^{at}] = \frac{1}{s-a}, \quad s-a > 0$

$$2. L[e^{-at}]$$

Soln, \rightarrow By definition of L.T

$$L[e^{-at}] = \int_0^{\infty} e^{-st} e^{-at} dt$$

$$= \int_0^{\infty} e^{-(s+a)t} dt = \left[\frac{e^{-(s+a)t}}{-(s+a)} \right]_0^{\infty}$$

$$= \frac{e^{-\infty}}{-(s+a)} - \frac{e^0}{-(s+a)}$$

$$= 0 + \frac{1}{s+a} \quad (\because e^{-\infty} = 0 \text{ \& } e^0 = 1)$$

$$= \frac{1}{s+a}$$

$$\therefore L[e^{-at}] = \frac{1}{s+a}, \quad s+a > 0$$

$$3) L[\cos at] \text{ and } L[\sin at]$$

Soln, \rightarrow We know that

$$e^{iat} = \cos at + i \sin at \quad (\because e^{it} = \cos t + i \sin t)$$

By definition of L.T

$$L[e^{iat}] = \int_0^{\infty} e^{-st} e^{iat} dt$$

$$= \int_0^{\infty} e^{-(s-ia)t} dt = \left[\frac{e^{-(s-ia)t}}{-(s-ia)} \right]_0^{\infty}$$

$$= \frac{e^{-\infty}}{-(s-ia)} - \frac{e^0}{-(s-ia)} = 0 + \frac{1}{s-ia}$$

$$= \frac{1}{s-ia} \quad (\because e^{-\infty} = 0 \text{ \& } e^0 = 1)$$

$$= \frac{1}{(s-ia)} \times \frac{(s+ia)}{(s+ia)}$$

$$= \frac{s+ia}{s^2-(ia)^2} = \frac{s+ia}{s^2+a^2}$$

$$L[e^{iat}] = \frac{s+ia}{s^2+a^2}$$

$$L[e^{iat}] = \frac{s}{s^2+a^2} + \frac{ia}{s^2+a^2}$$

$$L[\cos at] + iL[\sin at] = \frac{s}{s^2+a^2} + i\frac{a}{s^2+a^2}$$

Comparing real and imaginary parts, we get

$$L[\cos at] = \frac{s}{s^2+a^2} \text{ and } L[\sin at] = \frac{a}{s^2+a^2}$$

4) i) $L[\cosh at]$ ii) $L[\sinh at]$

Soln \rightarrow

As we know that $\cosh at = \frac{e^{at} + e^{-at}}{2}$

$$L[\cosh at] = \frac{1}{2} L[e^{at} + e^{-at}]$$

$$\begin{aligned} L[e^{at} + e^{-at}] &= \int_0^{\infty} e^{-st} [e^{at} + e^{-at}] dt \\ &= \int_0^{\infty} e^{-st} e^{at} + e^{-st} e^{-at} dt \\ &= \int_0^{\infty} e^{-(s-a)t} + e^{-(s+a)t} dt \end{aligned}$$

$$= \int_0^{\infty} e^{-(s-a)t} dt + \int_0^{\infty} e^{-(s+a)t} dt$$

$$= \left[\frac{e^{-(s-a)t}}{-(s-a)} \right]_0^{\infty} + \left[\frac{e^{-(s+a)t}}{-(s+a)} \right]_0^{\infty}$$

$$= \left[\frac{e^{-\infty}}{-(s-a)} - \frac{e^0}{-(s-a)} \right] + \left[\frac{e^{-\infty}}{-(s+a)} - \frac{e^0}{-(s+a)} \right]$$

$$= \frac{1}{s-a} + \frac{1}{s+a}$$

$$= \frac{s+a + s-a}{(s+a)(s-a)}$$

$$L[e^{at} + e^{-at}] = \frac{2s}{(s+a)(s-a)} = \frac{2s}{s^2 - a^2}$$

$$L[\cosh at] = \frac{1}{2} [e^{at} + e^{-at}]$$

$$= \frac{1}{2} \frac{2s}{s^2 - a^2}$$

$$\therefore L[\cosh at] = \frac{s}{s^2 - a^2}$$

i) We know that $\sinh at = \frac{e^{at} - e^{-at}}{2}$

$$L(\sinh at) = \frac{1}{2} L[e^{at} - e^{-at}]$$

$$L[e^{at} - e^{-at}] = \int_0^{\infty} e^{-st} [e^{at} - e^{-at}] dt$$

$$= \int_0^{\infty} e^{-st} e^{at} - e^{-st} e^{-at} dt$$

$$= \int_0^{\infty} e^{-(s-a)t} - e^{-(s+a)t} dt$$

$$\begin{aligned}
&= \int_0^{\infty} e^{-(s-a)t} dt - \int_0^{\infty} e^{-(s+a)t} dt \\
&= \left[\frac{e^{-(s-a)t}}{-(s-a)} \right]_0^{\infty} - \left[\frac{e^{-(s+a)t}}{-(s+a)} \right]_0^{\infty} \\
&= \frac{e^{-\infty}}{-(s-a)} - \frac{e^0}{-(s-a)} - \frac{e^{-\infty}}{-(s+a)} + \frac{e^0}{-(s+a)} \\
&= 0 + \frac{1}{s-a} - \frac{1}{s+a} \\
&= \frac{s+a + s-a}{s^2 - a^2} = \frac{2a}{s^2 - a^2}
\end{aligned}$$

$$L[\sinh at] = \frac{1}{2} \frac{2a}{s^2 - a^2}$$

$$\therefore L[\sinh at] = \frac{a}{s^2 - a^2}$$

$$\text{ss } L[t^n], \quad n \geq 0$$

Soln, \rightarrow By definition of L.T.

$$\begin{aligned}
L[t^n] &= \int_0^{\infty} e^{-st} t^n dt \\
&= \left[t^n \frac{e^{-st}}{-s} \right]_0^{\infty} - \int_0^{\infty} \frac{e^{-st}}{-s} n t^{n-1} dt
\end{aligned}$$

$$\begin{aligned}
&= 0 + \frac{n}{s} \int_0^{\infty} e^{-st} t^{n-1} dt \\
&= \frac{n}{s} L[t^{n-1}]
\end{aligned}$$

$$\text{Now } L[t^{n-1}] = \int_0^{\infty} e^{-st} t^{n-1} dt$$

Integrating by parts

$$\begin{aligned}L[t^{n-1}] &= \left. t^{n-1} \frac{e^{-st}}{-s} \right|_0^\infty - \int_0^\infty \frac{e^{-st}}{-s} (n-1) t^{n-2} dt \\&= 0 + \frac{n-1}{s} \int_0^\infty e^{-st} t^{n-2} dt \\&= \frac{n-1}{s} L[t^{n-2}] \\L[t^{n-1}] &= \frac{n(n-1)}{s^2} L[t^{n-2}]\end{aligned}$$

Continuing this process we get.

$$\begin{aligned}L[t^n] &= \frac{n(n-1)(n-2)(n-3)\dots 3 \times 2 \times 1}{s^n} L[t^0] \\&= \frac{n!}{s^n} L[1]\end{aligned}$$

$$\begin{aligned}\therefore L[1] &= \int_0^\infty e^{-st} 1 dt = \left. \frac{e^{-st}}{-s} \right|_0^\infty = \frac{e^{-\infty}}{-s} - \frac{e^0}{-s} \\&= 0 + \frac{1}{s} \quad (\because e^{-\infty} = 0)\end{aligned}$$

$$\therefore L[1] = \frac{1}{s}$$

$$\therefore L[t^n] = \frac{n!}{s^n} \frac{1}{s} = \frac{n!}{s^{n+1}}$$

BLDE ASSOCIATION'S
S.B.ARTS AND K.C.P SCIENCE COLLEGE, VIJAYAPUR
DEPARTMENT OF MATHEMATICS

SEMINAR REPORT: 2015-16
(Even Semester)

The UG Department of Mathematics has conducted seminar
for B.Sc students.

Name of the student

- 1) Surarna Gidaganti
- 2) Roopanjali Bondarde
- 3) Shweta Shapeti

Seminar Topic

The sphere
Diff eq^{ns} of nth order
Laplace transform


Head of Department

H. O. D.
Department of Mathematics,
S. B. Arts & K. C. P. Science
College, Vijayapur.


Principal

Principal,
S. B. Arts & K. C. P. Science
College, Vijayapur.


IQAC, Co-ordinator

S. B. Arts & K. C. P. Science College,
Vijayapur.